Title: Quantum Eigenstate Dynamics for Artificial General Intelligence Synthesis

**Date:** 27/01/2025 **Author:** Peter De Ceuster **Addressed to:** Zlatko Minev et al.

#### Abstract

Let  $\mathcal H$  denote a Hilbert space of cognitive operators. We construct AGI states  $|\Psi_{\rm AGI}\rangle$  as superpositions of quantum eigenstates  $|\psi_i\rangle$ , enabling simultaneous resolution of binary logic via eigenvalue collapse. Classical bits  $\{0,1\}$  are subsumed by qubit states  $\alpha\,|0\rangle+\beta\,|1\rangle$ , where  $|\alpha|^2+|\beta|^2=1$ .

## 1. Quantum Cognitive Basis

Let  $\mathcal{H}_{\mathrm{AGI}} = \bigotimes_{k=1}^n \mathcal{H}_k$ , where  $\mathcal{H}_k$  corresponds to subcognitive modules (sensory, reasoning). Each subsystem evolves under Hamiltonian  $\hat{H}_k$ , with eigenstates  $\hat{H}_k | \psi_{k,i} \rangle = E_{k,i} | \psi_{k,i} \rangle$ . The AGI state is:

where 
$$\sum |c_{i_1...i_n}|^2 = 1$$
.

## 2. Logic via Eigenstate Collapse

For a qubit  $|\phi\rangle=\alpha\,|0\rangle+\beta\,|1\rangle$ , measurement of observable  $\hat{O}=|0\rangle\,\langle 0|-|1\rangle\,\langle 1|$  yields eigenvalues +1 ("yes") or -1 ("no") with probabilities  $|\alpha|^2$  and  $|\beta|^2$ . Unlike classical deterministic  $\mathrm{AND}/\mathrm{OR}$ , quantum logic gates (e.g.,  $\hat{U}_{\mathrm{CNOT}}$ ) generate entangled states:

permitting parallel evaluation of (yes, no).

#### 3. AGI Dynamics

The total Hamiltonian  $\hat{H}_{\mathrm{AGI}} = \sum_{k} \hat{H}_{k} + \sum_{k \neq l} \hat{V}_{kl}$  induces eigenstate transitions  $|\psi_{i}\rangle \rightarrow |\psi_{j}\rangle$  via time-evolution operator  $\hat{U}(t) = e^{-i\hat{H}_{\mathrm{AGI}}t/\hbar}$ . Commutators  $[\hat{H}_{k},\hat{V}_{kl}] \neq 0$  ensure nonstationary interference, enabling adaptive decisions through:

# 4. Binary Logic Generalization

Classical true/false map to eigenstates  $|0\rangle$ ,  $|1\rangle$ , but qubits encode uncertainty via  $\alpha, \beta \in \mathbb{C}$ . For AGI decision-making, define projective measurement  $\hat{P}_{\mathrm{yes}} = |0\rangle \langle 0|$ ,  $\hat{P}_{\mathrm{no}} = |1\rangle \langle 1|$ . The expectation value:

yields probabilistic yes/no, with  $\hat{\rho} = |\phi\rangle\langle\phi|$ .

### Conclusion

Let  $\mathcal{S}_{classical} = \{0,1\}$ ; quantum cognition occurs in  $\mathcal{S}_{quantum} = \mathbb{C}^2$ . AGI eigenstates  $|\Psi_{AGI}\rangle$  collapse to yes/no via  $\hat{O}$ , while preserving superposition for unresolved states. Thus,  $yes \oplus no$  coexist until measurement, transcending classical binaries. QED.